# Warm-up Maths Questions for A-level Physics (trigonometry) *ANSWERS*



## **BASIC TRIGONOMETRY**

1. Evaluate: sin(30°)

$$\sin 30^{\circ} = 0.50$$

2. Evaluate: cos(60°)

$$\cos 60^{\circ} = 0.50$$

3. Find  $\theta$ : If  $\sin(\theta)=0.5$  and  $0^{\circ} \le \theta \le 90^{\circ}$ 

$$\theta = 30^{\circ}$$

**4.** Find  $\theta$ : If  $\cos(\theta)=1/2$  and  $0^{\circ} \le \theta \le 90^{\circ}$ 

$$\theta = 60^{\circ}$$

**5.** Evaluate: tan(45°)

$$tan 45^{\circ} = 1.0$$

### INTERMEDIATE TRIGONOMETRY

**6.** Simplify:  $\sin(90^{\circ}-\theta)$ 

$$\sin (90^{\circ} - \theta) = \cos \theta$$

**7.** Solve for  $\theta$ :  $\cos(\theta) = \sqrt{3}/2$  and  $0^{\circ} \le \theta \le 360^{\circ}$ 

$$\cos \theta = \sqrt{\frac{3}{2}}$$
 = 30° or 330°

**8.** Simplify: 2sin(30°)·cos(30°)

$$2 \sin 30^{\circ} \cos 30^{\circ} = 2 \times 0.5 \times \cos 30^{\circ} = \cos 30^{\circ} = 0.866$$

\*in physics we don't tend to leave numbers as fractions. We prefer to leave them as decimals so that we can see the number of significant figures that are appropriate. In maths you may leave the answer as  $\sqrt{\frac{3}{2}}$ 

**9.** Find  $\theta$ : If  $\tan(\theta)=1$  and  $0^{\circ} \le \theta \le 360^{\circ}$ 

$$\theta = 45^{\circ}$$
 or  $\theta = 225^{\circ}$ 

**10.** Evaluate: sin(120°)

$$\sin 120^{\circ} = \cos 30^{\circ} = 0.866$$

# ADVANCED TRIGONOMETRY

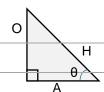
**11.** Solve for 
$$\theta$$
:  $2\sin(\theta) = 1$  and  $0^{\circ} \le \theta \le 360^{\circ}$ 

$$2 \sin \theta = 1$$

$$\sin \theta = \frac{1}{2}$$

$$\theta = 30^{\circ}$$
 or  $\theta = 150^{\circ}$ 

**12.** Prove the identity: 
$$\sin^2(\theta) + \cos^2(\theta) = 1$$



From the diagram: 
$$\sin \theta = O/H$$
 and so  $\sin^2 \theta = O^2 / H^2$ 

also: 
$$\cos \theta = A/H$$
 and so  $\cos^2 \theta = A^2/H^2$ 

Therefore: 
$$\frac{O^2}{H^2} + \frac{A^2}{H^2} = \frac{O^2 + A^2}{H^2}$$
 but from Pythagoras  $H^2 = O^2 + A^2$  so:  $\frac{O^2}{H^2} + \frac{A^2}{H^2} = 1$ 

13. Find x: If 
$$sin(x)=cos(x)$$
 and  $0^{\circ} \le x \le 90^{\circ}$ 

$$\sin x = \cos x$$

[but 
$$\sin \theta = \cos (90 - \theta)$$
]

So: 
$$\sin x = \cos (90-x)$$

and so 
$$x = 45^{\circ}$$

**14.** Solve for 
$$\theta$$
:  $\cos^2(\theta) = 1/4$  and  $0^\circ \le \theta \le 360^\circ$ 

$$\cos^2 \theta = \frac{1}{4}$$

$$\cos \theta = \sqrt{\frac{1}{4}}$$

so: 
$$\theta = 60^{\circ}$$
 or  $\theta = 300^{\circ}$ 

**15.** Evaluate: 
$$\cos^{-1}(1/2)$$

$$\cos^{-1} 0.5 = 60^{\circ}$$

# **COMPLEX TRIGONOMETRY**

**16.** Solve for 
$$\theta$$
:  $2\sin^2(\theta) - 1 = 0$  and  $0^\circ \le \theta \le 360^\circ$ 

$$\sin^2 \theta = 1/2$$

$$\sin \theta = \sqrt{1/2}$$

$$\theta = 45^{\circ}$$
 or  $\theta = 135^{\circ}$ ,  $\theta = 225^{\circ}$ ,  $\theta = 315^{\circ}$ 

17. Find the general solution: 
$$tan(\theta) = \sqrt{3}$$

$$\tan \theta = \sqrt{3}$$
 so  $\tan \theta = 60^{\circ}$ 

(for 
$$0^{\circ} \le \theta \le 180^{\circ}$$
)

For a general solution:

$$\tan \theta = 60^{\circ} + n180^{\circ}$$

[ later in your studies you will learn to write this as:  $\tan \theta = \pi/3 + n\pi$  ]

**18.** Simplify: 
$$\sin(2\theta) / \cos(\theta)$$

[for this question we can use the trigonometric identity  $\sin 2\theta = 2\sin\theta \cos\theta$ ]

$$\frac{\sin 2\theta}{\cos \theta} = \frac{2\sin \theta \cos \theta}{\cos \theta}$$

= 
$$2 \sin \theta$$

**19.** Solve for 
$$\theta$$
:  $2\cos(\theta)+1=0$  and  $0^{\circ} \le \theta \le 360^{\circ}$ 

$$\cos \theta = -\frac{1}{2}$$
 = 120° or 240°

**20.** Find 
$$\theta$$
:  $\sin(2\theta) = \cos(\theta)$  and  $0^{\circ} \le \theta \le 360^{\circ}$ 

$$2 \sin \theta \cos \theta = \cos \theta$$

$$2 \sin \theta = \cos \theta / \cos \theta = 1$$

$$\sin \theta = \frac{1}{2}$$

$$\theta = 30^{\circ} \text{ or } 150^{\circ}$$